Consider the following symmetric matrix:

1. Find the eigenvalues of S. Create a diagonal matrix D with the eigenvalues as the diagonal entries.
2. Find the eigenvectors of S. Demonstrate that they are orthogonal.
3. Normalize the eigenvectors to unit length and put them into the columns of a matrix Q.
4. Demonstrate that S can be written as: